Intermediate ALGEBRA with COVER Learning

Sherri Messersmith Lawrence Perez Robert S. Feldman



P.O.W.E.R. is an approach to systematically completing tasks based on five practical steps



The most critical facet of preparation is setting goals. Goal-setting improves student performance by increasing student focus, confidence, motivation, and persistence.



Students have to identify and organize the intellectual tools necessary to accomplish their goals. Organizing refers not only to considering how they must apply the most appropriate academic strategies, but also to maintaining and applying good habits outside of class in order to manage their many responsibilities.



Doing the work-reading the materials, taking good notes in class, and doing in-class exercises-may seem like the most obvious step, but it is an area where students often falter. Using P.O.W.E.R. will improve your students' motivation and help them view success as a product of their hard work and effort.



In math, concepts build on each other, so student success depends on reaching a level of mastery in each section before progressing. P.O.W.E.R. helps students understand that their work is not complete until they have assessed their progress and identified where they are struggling.



Too often in developmental math, students do not stop to assess their overall performance until after an exam, at which point it may be too late. P.O.W.E.R. prompts students after each section to honestly assess how they are doing and where they may need to change their strategy or ask for help.

Why Math Needs



The P.O.W.E.R. series is a solution for students struggling to achieve their academic goals and instructors trying to balance teaching math with teaching effective student behavior.



Sherri Messersmith Professor of Mathematics, College of DuPage

"Developmental students don't *want* to fail, they just don't know how to succeed. Teaching students at the developmental level is not just about teaching mathematics; it's about helping them learn all of the 'other' things it takes to be successful in college (and in life). If students don't know how to read a textbook, how to manage their time, how to take notes, how to set realistic goals, how to study, etc.—if they don't know how to be college students, then how can they be successful in our math courses? This challenge for students becomes our challenge as instructors. How do we teach successful student behavior while also getting through the objectives in our math courses?"

"First and foremost, this is a math textbook. Its purpose is to present all of the mathematics that is required for a course in the clearest, most mathematically precise way possible through the use of both traditional methods and some that you will find unique. But we think it is crucial to address study strategies as well, and, in fact, Larry and I wrote the manuscripts this way even before we met Bob! We teamed up to formalize the steps by integrating the P.O.W.E.R. framework into the textbooks, customizing it for teaching and learning mathematics. It turned out to be a very natural fit."



Lawrence Perez

Professor of Mathematics, Saddleback College

"It's not just about the content. Having an easy-to-read text coupled with thought-provoking pedagogy, in many cases, is not enough. As instructors, we strive to teach our students how to be successful learners. Integrating study strategies that are not directly connected to the text may not suffice. This is what makes the P.O.W.E.R. Math Series different. Dr. Feldman's research has provided the necessary framework that can assist developmental math students in navigating the difficult transition from arithmetic to abstract algebra and it is applicable to a variety of learning environments. It is also a framework that we as developmental math instructors can use to create our own supplemental resources and refine our personal teaching styles."



Bob Feldman

Dean and Professor of Psychology, University of Massachusetts Amherst, Director of POWER Up for Student Success, The UMass first-year experience program

"Good students are made, not born. What does being a 'good' student at the college level mean? Among other things, it means coming to class prepared, taking good notes, developing good study habits, and managing time effectively. These skills can be taught, and taught in ways that lead to success. In fact, careful research shows courses that cover the skills related to college success produce a significant and demonstrable rise in student retention beyond the first semester in college. After years of teaching and doing research in student success, I developed the P.O.W.E.R. Learning framework to help students to achieve their goals in any class and even after they graduate."

"A developmental math course is often one of the first courses students take at the college level, and it is the gateway to continuing their college education. We have integrated a proven method of helping students develop basic skills into a text written by instructors with years of classroom experience."

What Students Are Saying about



Dozens of college students participated in focus groups to help develop this series. Here is what they told us. To see video clips of students talking about P.O.W.E.R. go to www.mhhe.com/sem/powermath

"In math class, I usually dive head first into the problems, hoping the material will come to me. I don't evaluate my work which leads to dishonesty about my strengths and weaknesses and whether I understand the concepts enough to move on. The "Evaluate" step in P.O.W.E.R. will really help improve my grades."

– Ashley Grayson, Northeastern Illinois University

"P.O.W.E.R. will help prepare me to do or learn something that is a little challenging. It helps me identify my goals and what I need to do to get there."

– Nina Turnage, Wilbur Wright College

"I always work in a trial and error kind of way. P.O.W.E.R. will help me study more efficiently because it breaks down learning into steps." – Zainab Khomusi, University of Illinois at Chicago



"The P.O.W.E.R. framework is like the scientific method for learning. Even outside of class, I think it will help me be successful in business and life goals." – Nathan Hurde, University of Illinois at Chicago

"You can use P.O.W.E.R. to attack learning math, or really any subject, successfully." – Eire Aatnite, *Roosevelt University*

"P.O.W.E.R. would motivate and guide me to take more time with math and **recognize and fix my weaknesses.**"

– Jaimie O'Leary, Northeastern Illinois University

"I like that this framework already fits in with a lot of my study habits. It just makes sense."

- Lauren Mosley, Western Illinois University

Geometry Formulas



Intermediate ALGEBRA



INTERMEDIATE ALGEBRA WITH P.O.W.E.R. LEARNING

Published by McGraw-Hill, a business unit of The McGraw-Hill Companies, Inc., 1221 Avenue of the Americas, New York, NY 10020. Copyright © 2014 by The McGraw-Hill Companies, Inc. All rights reserved. Printed in the United States of America. No part of this publication may be reproduced or distributed in any form or by any means, or stored in a database or retrieval system, without the prior written consent of The McGraw-Hill Companies, Inc., including, but not limited to, in any network or other electronic storage or transmission, or broadcast for distance learning.

Some ancillaries, including electronic and print components, may not be available to customers outside the United States.

This book is printed on acid-free paper.

1 2 3 4 5 6 7 8 9 0 DOW/DOW 1 0 9 8 7 6 5 4 3

ISBN 978-0-07-340627-5 MHID 0-07-340627-9

ISBN 978–0–07–748378–4 (Annotated Instructor's Edition) MHID 0–07–748378–2

Senior Vice President, Products & Markets: Kurt L. Strand Vice President, General Manager, Products & Markets: Marty Lange Vice President, Content Production & Technology Services: Kimberly Meriwether David Managing Director: Rvan Blankenship Director, Developmental Mathematics: Dawn R. Bercier Director of Development: Rose Koos Director of Digital Content: Nicole Lloyd Development Editors: Liz Recker / Elizabeth O'Brien Market Development Manager: Kim Leistner Marketing Director: Alex Gav Director, Content Production: Terri Schiesl Lead Project Manager: Peggy J. Selle Buyer: Nicole Baumgartner Senior Media Project Manager: Sandra M. Schnee Senior Designer: David W. Hash Cover/Interior Designer: Rokusek Design, Inc. Cover Image: Power button icon © tkemot Lead Content Licensing Specialist: Carrie K. Burger Compositor: *Aptara*[®], *Inc.* Typeface: 10/13 Times New Roman MT Std Printer: R. R. Donnellev

All credits appearing on page or at the end of the book are considered to be an extension of the copyright page.

Library of Congress Cataloging-in-Publication Data

Cataloging-in-Publication Data has been requested from the Library of Congress.

Intermediate ALGEBRA

SHERRI MESSERSMITH College of DuPage

LAWRENCE PEREZ Saddleback College

ROBERT S. FELDMAN University of Massachusetts Amherst

With contributions from William C. Mulford, The McGraw-Hill Companies

About the Authors

Sherri Messersmith

Professor of Mathematics, College of DuPage

Sherri Messersmith began teaching at the College of DuPage in Glen Ellyn, Illinois in 1994 and has over 25 years of experience teaching many different courses from developmental mathematics through calculus. She earned a Bachelor of Science degree in the Teaching of Mathematics at the University of Illinois at Urbana-Champaign and taught at the high school level for two years. Sherri returned to UIUC and earned a Master of Science in Applied Mathematics and stayed on at the university to teach and coordinate large sections of undergraduate math courses as well as teach in the Summer Bridge program for at-risk students. In addition to the P.O.W.E.R. Math Series, she is the author of a hardcover series of textbooks and has also appeared in videos accompanying several McGraw-Hill texts.

Sherri and her husband are recent empty-nesters and live in suburban Chicago. In her precious free time, she likes to read, cook, and travel; the manuscripts for her books have accompanied her from Spain to Greece and many points in between.

Lawrence Perez

Professor of Mathematics, Saddleback College

Larry Perez has fifteen years of classroom experience teaching math and was the recipient of the 2010 Community College Professor of the Year Award in Orange County, California. He realized early on that students bring to the classroom different levels of attitude, aptitude, and motivation sometimes accompanied by a tremendous fear of taking math. Confronted by this, he developed a passion for engaging students, demanding him to innovate traditional and online pedagogical techniques using architecture created with student feedback as the mechanism of design. He is the creator of the award-winning online learning environment Algebra2go[®] and has presented his work and methodology at conferences around the country.

Larry is a Veteran of the United States Navy Submarine Force and is a graduate of California State University Fullerton earning degrees in Electrical Engineering and Applied Mathematics. In his spare time he enjoys mountain biking and the great outdoors.

Robert S. Feldman

Dean and Professor of Psychology, University of Massachusetts Amherst

Bob Feldman still remembers those moments of being overwhelmed when he started college at Wesleyan University. "I wondered whether I was up to the challenges that faced me," he recalls, "and although I never would have admitted it then, I really had no idea what it took to be successful at college."

That experience, along with his encounters with many students during his own teaching career, led to a life-long interest in helping students navigate the critical transition that they face at the start of their own college careers. Bob, who went on to receive a doctorate in psychology from the University of Wisconsin-Madison, teaches at the University of Massachusetts Amherst, where he is the Dean of the College of Social and Behavioral Sciences and Professor of Psychology. He also directs a first-year experience course for incoming students.

Bob is a Fellow of both the American Psychological Association and the Association for Psychological Science. He has written more than 200 scientific articles, book chapters, and books, including P.O.W.E.R. Learning: *Strategies for Success in College and Life*, 6e and *Understanding Psychology*, 11e. He is president-elect of the FABBS Foundation, an umbrella group of societies promoting the behavioral and brain sciences.

Bob loves travel, music, and cooking. He and his wife live near the Holyoke mountain range in western Massachusetts.

Table of Contents

CHAPTER 1

Real Numbers and Algebraic Expressions 1

Study Strategies: The P.O.W.E.R. Framework 2

- Section 1.1 Set of Numbers 4
- Section 1.2 Operations on Real Numbers 12
- Section 1.3 Exponents, Roots, and Order of
- Operations 20 Section 1.4 Algebraic Expressions and
- Properties of Real Numbers 26 Group Activity 30 emPOWERme: Why Am I Going to College? 31 Chapter 1 Summary 32 Chapter 1 Review Exercises 34 Chapter 1 Test 35

CHAPTER 2

Linear Equations in One Variable 36

Study Strategies: Reading Math (and Other) Textbooks 37

- Section 2.1 Linear Equations in One Variable 39
- Section 2.2 Applications of Linear Equations 52
- Section 2.3 Geometry Applications and Solving Formulas 66
- Section 2.4 More Applications of Linear Equations 76 Group Activity 85 emPOWERme: Organize Your Memory 86 Chapter 2 Summary 88 Chapter 2 Review Exercises 90 Chapter 2 Test 92 Cumulative Review for Chapters 1 and 2 93

CHAPTER 3 Linear Inequalities and Absolute Value 94

Study Strategies: Time Management 95

- Section 3.1 Linear Inequalities in One Variable 97
- Section 3.2 Compound Inequalities in One Variable 109
- Section 3.3 Absolute Value Equations and Inequalities 117 Group Activity 129 emPOWERme: Identify the Black Holes of Time Management 129 Chapter 3 Summary 131 Chapter 3 Review Exercises 132 Chapter 3 Test 133 Cumulative Review for Chapters 1–3 134

PTER 4	Linear Equations in Two Variables and Functions 135
Study Strate	gies: Taking Notes in Class 136
Section 4.1	Introduction to Linear Equations in Two Variables 138
Section 4.2	Slope of a Line and Slope-Intercept Form 155
Section 4.3	Writing an Equation of a Line 170
Section 4.4	Linear and Compound Linear Inequalities in Two Variables 186
Section 4.5	Introduction to Functions 196
	Group Activity 213 emPOWERme: Checklist for Effective Notes 214 Chapter 4 Summary 215 Chapter 4 Review Exercises 221 Chapter 4 Test 225 Cumulative Review for Chapters 1–4 227
PTER 5	Solving Systems of Linear

Equations 228

Study Strategies: Taking Math Tests 229

Section 5.1	Solving Systems of Linear Equations in Two Variables 232	
Section 5.2	Solving Systems of Linear Equations in Three Variables 250	
Section 5.3	Applications of Systems of Linear Equations 259	
Section 5.4	Solving Systems of Linear Equations Using Matrices 273 Group Activity 281	
	emPOWERme: Studying Smart 281 Chapter 5 Summary 282	
	Chapter 5 Review Exercises 286 Chapter 5 Test 288	
	Cumulative Review for	

CHAPTER 6

CHA

CHA

Polynomials and Polynomial Functions 290

Study Strategies: Doing Math Homework 291

Chapters 1-5 289

Section 6.1	The Rules of Exponents 293
Section 6.2	More on Exponents and Scientific
	Notation 303
Section 6.3	Addition and Subtraction of
	Polynomials and Polynomial
	Functions 313
Section 6.4	Multiplication of Polynomials and
	Polynomial Functions 324

Section 6.5 Division of Polynomials and Polynomial Functions 335 Group Activity 344 emPOWERme: The Right Time and Place for Homework 335 Chapter 6 Summary 346 Chapter 6 Review Exercises 348 Chapter 6 Test 351 **Cumulative Review for** Chapters 1-6 352

CHAPTER 7

Factoring Polynomials 353

Study Strategies: Working with a Study Group 354

Section	7.1	The Greatest Common Factor and	
		Factoring by Grouping 356	
Section	7.2	Factoring Trinomials 366	
Section	7.3	Special Factoring Techniques	378

- Putting It All Together 388 Section 7.4 Solving Quadratic Equations by
- Factoring 392 Section 7.5 Applications of Quadratic
 - Equations 402 Group Activity 412 emPOWERme: Switch "You" to "l" 413 Chapter 7 Summary 414 Chapter 7 Review Exercises 416 Chapter 7 Test 418 **Cumulative Review for** Chapters 1-7 419

CHAPTER 8 Rational Expressions, Equations, and Functions 420

Study Strategies: The Writing Process 421 Section 8.1 Simplifying, Multiplying, and Dividing Rational Expressions and Functions 423 Section 8.2 Adding and Subtracting Rational Expressions 436 Section 8.3 Simplifying Complex Fractions 450 Section 8.4 Solving Rational Equations 460 Putting It All Together 471 Section 8.5 Applications of Rational Equations 478 Section 8.6 Variation 488 Group Activity 496 emPOWERme: Mad, Mad, Mad Math 496 Chapter 8 Summary 497 Chapter 8 Review Exercises 502 Chapter 8 Test 505 **Cumulative Review for** Chapters 1-8 506

CHAPTER 9 Radicals and Rational

Exponents 507

Study Strategies: Working with Technology 508 Section 9.1 Radical Expressions and Functions 511 Section 9.2 Rational Exponents 525 Section 9.3 Simplifying Expressions Containing Square Roots 534 Section 9.4 Simplifying Expressions Containing Higher Roots 545 Section 9.5 Adding, Subtracting, and Multiplying Radicals 553 Section 9.6 Dividing Radicals 561 Putting It All Together 573 Section 9.7 Solving Radical Equations 578 Section 9.8 Complex Numbers 587 Group Activity 596 emPOWERme: Information Please! 597 Chapter 9 Summary 598 Chapter 9 Review Exercises 603 Chapter 9 Test 605 Cumulative Review for Chapters 1–9 606

CHAPTER 10 **Quadratic Equations and** Functions 607

Study Strategies: Developing Financial Literacy 608

- Section 10.1 The Square Root Property and Completing the Square 610
- Section 10.2 The Quadratic Formula 623 Putting It All Together 632
- Section 10.3 Equations in Quadratic Form 636
- Section 10.4 Formulas and Applications 645 Section 10.5 Quadratic Functions and their
- Graphs 653 Section 10.6 Application of Quadratic Functions and Graphing Other Parabolas 667
- Section 10.7 Quadratic and Rational Inequalities 680 Group Activity 690 emPOWERme: Determine Your Saving Style 691 Chapter 10 Summary 692 Chapter 10 Review Exercises 696 Chapter 10 Test 699 Cumulative Review for Chapters 1–10 700

CHAPTER 11

Exponential and Logarithmic Functions 701

Study Strategies: Coping with Stress 702 Section 11.1 Composite and Inverse Functions 704 Section 11.2 Exponential Functions 719

Section 11.3Logarithmic Functions730Section 11.4Properties of Logarithms743

Section 11.5 Common and Natural Logarithms and Change of Base 753 Section 11.6 Solving Exponential and Logarithmic Equations 765 Group Activity 776 emPOWERme: Progressive Relaxation 777 Chapter 11 Summary 778 Chapter 11 Review Exercises 783 Chapter 11 Test 786 Cumulative Review for Section 12.5 Nonlinear Systems of Equations 832 Section 12.6 Second-Degree Inequalities and Systems of Inequalities 839 Group Activity 844 emPOWERme: Memory Devices 845 Chapter 12 Summary 846 Chapter 12 Review Exercises 849 Chapter 12 Test 850 Cumulative Review for Chapters 1–12 851

APPENDIX

Section A.1	Review of Fractions A-1
Section A.2	Geometry Review A-12
Section A.3	Determinants and Cramer's Rule A-24
Section A.4	Synthetic Division and the Remainder Theorem A-33
This appendix is www.connectmat	available online at h.com and www.mcgrawhillcreate.com

Student Answer Appendix SA-1 Instructor Answer Appendix (AIE only) IA-1 Credits C-1 Index I-1

CHAPTER 12 Nonlinear Functions, Conic Sections, and Nonlinear Systems 788

Chapters 1–11 787

Study Strategies: Improving Your Memory 789 Section 12.1 Graphs of Other Useful

- Functions 791 Section 12.2 The Circle 802
- Section 12.3 The Ellipse 810
- Section 12.4 The Hyperbola 817 Putting It All Together 828

Consistent Integration of Study Skills

In *Intermediate Algebra*, strategies for learning are presented alongside the math content, making it easy for students to learn math *and* study skills at the same time. The P.O.W.E.R. framework aligns with the math learning objectives, providing instructors with a resource that has been consistently integrated throughout the text.

A **STUDY STRATEGIES** feature begins each chapter. Utilizing the P.O.W.E.R. framework, these boxes present steps for mastering the different skills students will use to succeed in their developmental math course. For example, these boxes will contain strategies on time management, taking good notes and, as seen in the sample below, taking a math test.



CHAPTER AND SECTION POWER PLANS Before getting started on reading the chapter, a student will focus on Preparation and Organization skills in the **POWER Plans**. These tools give practical suggestions for setting and achieving goals. The steps revolve around best practices for student success and then apply P.O.W.E.R. toward learning specific concepts in math.

Chapter 5 Plan

Prepare	Organize
What are your goals for Chapter 5?	How can you accomplish each goal?
1 Be prepared before and during class.	 Don't stay out late the night before, and be sure to set your alarm clock! Bring a pencil, notebook paper, and textbook to class. Avoid distractions by turning off your cell phone during class. Pay attention, take good notes, and ask questions. Complete your homework on time, and ask questions on problems you do not understand. Plan ahead for tests by preparing many days in advance.
2 Understand the homework to the point where you could do it without needing any help or hints.	 Read the directions, and show all of your steps. Go to the professor's office for help. Rework homework and quiz problems, and find similar problems for practice. Review old material that you have not mastered yet.
3 Use the P.O.W.E.R. framework to help you take tests: <i>Studying Smart.</i>	 Read the Study Strategy that explains how to study effectively for tests. Do a "practice run" the night before the test by doing a practice test without notes. Complete the emPOWERme that appears before the Chapter Summary.
4 Write your own goal.	•
What are your objectives for Chapter 5?	How can you accomplish each objective?
1 Be able to solve a system of linear equations in two variables by using the graphing, substitution, or elimination methods. Know when to use each method.	 Learn the procedures for each of these methods. Know the terminology associated with the solutions such as independent and consistent. Know how to check each answer.
2 Be able to determine when the solution to a system of equations is <i>no solution</i> or <i>infinite solutions</i> . Know what these solutions look like on a graph and how to write the answer.	 Learn the procedures for solving a system of equations and the possible answers when variables "drop out." Learn the terminology associated with the solutions such as <i>inconsistent</i> and <i>dependent</i>. Know what these results look like on a graph. Know how to check your solutions.
3 Be able to solve a system of linear equations in three variables, including systems where there are missing terms.	 Learn the procedure for Solving a System of Linear Equations in Three Variables. Know how to check your solutions.

Be sure you are writing out each step as you are reading the example.	b) To solve $t^2 - 20 = 0$, begin by getting t^2 on a side by itself. $t^2 - 20 = 0$ $t^2 = 20$ $t = \pm \sqrt{20}$ Add 20 to each side. $t = \pm \sqrt{20}$ Square root property $t = \pm \sqrt{4} \cdot \sqrt{5}$ Product rule for radicals $t = \pm 2\sqrt{5}$ $\sqrt{4} = 2$	
	Check: $t = 2\sqrt{5}$: $t^2 - 20 = 0$ $(2\sqrt{5})^2 - 20 \stackrel{?}{=} 0$ $(4 \cdot 5) - 20 \stackrel{?}{=} 0$ $20 - 20 = 0$ $(-2\sqrt{5})^2 - 20 \stackrel{?}{=} 0$ $(4 \cdot 5) - 20 \stackrel{?}{=} 0$ $20 - 20 = 0$ \checkmark	
	The solution set is $\{-2\sqrt{5}, 2\sqrt{5}\}$.	

WORK HINTS provide additional explanation and point out common places where students might go wrong when solving a problem. Along with the *Be Careful* boxes, these tools act as a built-in tutor, helping students navigate the material and learn concepts even outside of class.

IN-CLASS EXAMPLES are available only in the Annotated Instructor Edition. These examples offer instructors additional problems to work through in class. In-class example problems align with the Guided Student Notes resource available with this package.

EXAMPLE 1	Solve using the square root property. a) $x^2 = 9$ b) $t^2 - 20 = 0$ c) $2a^2 + 21 = 3$	
	Solution	
	a) $x^2 = 9$ $x = \sqrt{9}$ or $x = -\sqrt{9}$ Square root property x = 3 or $x = -3$	
The solution set is $\{-3, 3\}$. The check is left to the student.		
An equivalent way to solve $x^2 = 9$ is to write it as		
	$x^{2} = 9$ $x = \pm \sqrt{9}$ Square root property $x = \pm 3$	
	The solution set is $\{-3, 3\}$. We will use this approach when solving equations using the square root property.	

PUTTING IT ALL TOGETHER One of the challenges students struggle with is putting all of the steps they've learned together and *applying* that knowledge to a problem. *Putting It All Together* sections will help students understand the big picture and work through the toughest challenge when solving applications—*problem recognition,* or knowing *when* to use *what* method or thought process. These sections include a summary and several problems that help students reason through a problem using conversational, yet mathematically correct, language.

Putting It All Together

What are your objectives for Putting It All Together?	How can you accomplish each objective?
 Decide Which Method to Use to Solve a Quadratic Equation 	 Be able to write out all the different methods in your notes. Review characteristics of each method, and be able to identify the most efficient method for each problem. Try solving some problems using more than one method, if time permits, and check your answers. Complete the given example on your own.

em **POWER** me Studying Smart

Imagine packing your bag for a trip without knowing where you were going. Would you take sweaters or swimsuits? A raincoat or sunblock? This dilemma is parallel to the one you face if you study for a test without knowing what it will cover. The key to effective studying—and to successful test-taking—is to tailor your efforts to the test you will have to take. Before you start studying, answer these questions, and use your answers to help you prepare.

- Is the test called a "test," "exam," "quiz," or something else? There is a difference! Exams tend to be longer, while quizzes are often shorter and narrower in their focus. If you are aren't sure, ask your instructor.
- What material will the test cover? Will it cover only the most recent subjects or everything you've learned in the term so far?
- How many questions will be on the test? How much time is it expected to take? A full class period? Only part of a period?
- What kinds of questions will be on the test?
- Will you be allowed to use a calculator? Consult your textbook?
- Will the test be graded on a curve?
- Will sample questions be provided?
- Are tests from previous terms available for you to study?
- How much does the test contribute to your final course grade?

emPOWERme boxes circle back to the opening Study Strategies and give students a checklist to evaluate how well they followed through on all of the positive habits recommended to successfully master a skill.

Instructor **POWER** Tool Kit

The Messersmith/Perez/Feldman Series offers instructors a robust digital resources package to help you with all of your teaching needs.

Resources in your P.O.W.E.R. tool kit include: Connect Hosted by Aleks* •

- **ALEKS 360*** •
- Instructor Solutions Manual
- Student Solutions Manual
- Guided Student Notes*
- Classroom Worksheets*
- Instructor Resource Manual •
- Test Bank Files
- Computerized Test Bank
- Faculty Development and Digital Training*
- PowerPoint Presentations
- Extensive Video Package*

*Details of these resources are included in the following pages!

Videos

Hundreds of videos are available to guide students through the content, offering support and instruction even outside vour classroom.

Exercise Videos – These 3–5-minute clips show students how to solve various exercises from the textbook. With around thirty videos for every chapter, your students are supported even outside the classroom.

Lecture Videos – These 5–10-minute videos walk students through key learning objectives and problems from the textbook.

P.O.W.E.R. Videos – These engaging segments guide students through the P.O.W.E.R. framework and the study skills for each chapter.

Perform the operations and simplify: $4 - \sqrt{13} + 8 - 6\sqrt{13}$ Like radicals have the same index and the same radicand.

> $4 - \sqrt{13} + 8 - 6\sqrt{13}$ $12 - \sqrt{13} - 6\sqrt{13}$ $12 + (-1 - 6)\sqrt{13}$ $12 + (-7)\sqrt{13}$ $12 - 7\sqrt{13}$

12 - 7 times square root (13).

Faculty Development and Digital Training

McGraw-Hill is excited to partner with our customers to ensure success in the classroom with our course solutions.



Workshops are available on these topics for anyone using or considering the Messersmith/Perez/Feldman P.O.W.E.R. Math Series. Led by the authors, contributors, and McGraw-Hill P.O.W.E.R. Learning consultants, each workshop is tailored to the needs of individual campuses or programs.

New to McGraw-Hill Digital Solutions? Need help setting up your course, using reports, and building assignments?

No need to wait for that big group training session during faculty development week. The McGraw-Hill Digital Implementation Team is a select group of advisors and experts in Connect Hosted by ALEKS[™]. The Digital Implementation Team will work one-on-one with each instructor to make sure you are trained on the program and have everything you need to ensure a good experience for you and your students.





Are you redesigning a course or expanding your use of technology? Are you interested in getting ideas from other instructors who have used ALEKS[™] or Connect Hosted by ALEKS in their courses?

Digital Faculty Consultants (DFCs) are instructors who have effectively incorporated technology such as ALEKS and Connect Hosted by ALEKS Corp. in their courses. Discuss goals and best practices and improve outcomes in your course through peer-to-peer interaction and idea sharing.

Contact your local representative for more information about any of the faculty development, training, and support opportunities through McGraw-Hill. <u>http://catalogs.mhhe.com/mhhe/findRep.do</u>

GUIDED STUDENT NOTES

By taking advantage of Guided Student Notes, your students will have more time to learn the material and participate in solving in-class problems while, at the same time, becoming better note takers. Ample examples are included for appropriate coverage of a topic that will not overwhelm students. Use them as they are or download and edit the Guided Student Notes according to your teaching style.

Guided Student Notes MPF – Intermediate Algebra Rules for Dividing Rational Expressions	
Divide. Write each rational expression in lowest terms.	Guided Student Notes Name: MPF – Intermediate Algebra
$16) \frac{42b^\circ}{c^3} \div \frac{2b}{c^5}$	8.1 Simplifying, Multiplying, and Dividing Rational Expressions and Functions Prepare What are my goals for this section?
$17) \frac{r^2 - 13r + 36}{2r + 10} \div \frac{12r - 3r^2}{16}$	Organize What am I going to do to accomplish these goals?
	Work Definition of a Rational Expression Definition of a Rational Function
$18) \ \frac{3n^2 - 22n - 16}{n^2} + (3n + 2)^2$	Determining the Domain of a Rational Function
5	1) If $f(x) = \frac{x^2 - 16}{x + 3}$, a) find $f(5)$
	 b) find x so that f(x)=0 c) determine the domain of the function.
	1

WORKSHEETS FOR STUDENT AND INSTRUCTOR USE

Worksheets for every section are available as an instructor supplement. These author-created worksheets provide a quick, engaging way for students to work on key concepts. They save instructors from having to create their own supplemental material and address potential stumbling blocks in student understanding. Classroom tested and easy to implement, they are also a great resource for standardizing instruction across a mathematics department.

The worksheets fall into three categories: Worksheets to Improve Basic Skills; Worksheets to Help Teach New Concepts; and Worksheets to Tie Concepts Together.

The worksheets are available in an instructor edition, with answers, and in a student edition, without answers.

	Worksheet 5A Name: Messersmith – Intermediate Algebra	-
	Evaluate.	
Worksheet 5A Massarsmith - Intermediate Algebra	1) √36 16) √64	
Evaluate.	2) $\sqrt{144}$ 17) $\sqrt[3]{32}$	
1) √ <u>36</u> <u>6</u>	3) $\sqrt{25}$ 18) $\sqrt{49}$	
2) √ <u>144</u> <u>12</u>	4) √8 19) √100	
3) √ <u>25</u> <u>5</u>	5) ∛125 20) ∛8	
4) ∛8 2	6) √81 21) ∜1	
5) ∛ <u>125</u> <u>5</u>	7) √27 22) √27	
6) √ <u>81</u> <u>9</u>	8) $\sqrt[4]{16}$ 23) $\sqrt{16}$	
7) ∛ <u>27</u> _ 3	9) $\sqrt[3]{1000}$ 24) $\sqrt[3]{32}$	
8) ∜ <u>16</u> _2	10) $\sqrt{121}$ 25) $\sqrt{121}$	
9) ∛1000 <u>10</u>	11) √169 26) ∜81	
10) √ <u>121</u> <u>11</u>	12) ∜64 27) ∛125	
11) √169 13	13) $\sqrt[4]{81}$ 28) $\sqrt[4]{16}$	
12) \$\sqrt{64} _2	14) $\sqrt{4}$ 29) $\sqrt{9}$	
13) ∜81	15) ∛ĩ 30) √ĩ	
14) $\sqrt{4}$	27) X7	
15) ∜ī <u>1</u>	30) √ī <u>1</u>	

Connect Math Hosted by ALEKS[®] Corp.

Built By Today's Educators, For Today's Students

Fewer clicks means more time for you...





CONNECT MATH

xvi

www.successinmath.com

Quality Content For Today's Online Learners

Online Exercises were carefully selected and Question 16 of 26 (1 point) 6.4 Section Exercise 48 Write the percent equation in terms of x. Then solve for the unknown percent. Round to the Try Another developed to provide a seamless transition nearest tenth of a percent if necessary. Solve It from textbook to technology. What percent of 80 is 4.24? Step 1: Show Example Let x represent the unknown percent. Ask My Instructor $\begin{array}{c|c} \underline{\text{What percent}} & \text{of} & 80 & \text{is} & 4.24? \\ \downarrow & \downarrow & \downarrow & \downarrow \\ x & (\text{select}) \bullet (80) & (\text{select}) \bullet & 4.24 \end{array}$ Link to Textbook Question 20 of 29 (1 point) 2.7 Section Exercise 42 Two canoes travel down a river, starting at 9:00 A.M. One canoe travels twice as fast as the Try Another other. After 4.5 hr. the canoes are 15.75 mi apart. Find the speed of each canoe. Solve It Step 1: Read the problem and draw a sketch. Show Example For simplicity, we will call the two canoes, Canoe A and Canoe B. Let Canoe B be the canoe that Ask My Instructor travels at the faster rate Link to Textbook 15.75 mi Step 2: Label the variables. connect Let x represent the rate of Canoe A Then, 2x is the rate of Canoe B. og 🕫 book conferts 🗃 🖌 🧮 🔛 🚔 🚳 search ebeek 🕫 To complete the second column, we can use the relationship, d = rtDistance Rate Time chapter 6. Factoring Polynomials Title: Hornew Type: Online
 Canoe A
 4.5x
 x
 4.5

 Canoe B
 4.5(____)
 2x
 4.5
 6 For consistency, the guided solutions match the style and voice of the original text as though the author is guiding the students through the problems. Multimedia eBook includes access to a variety of media assets and a place to highlight and keep track of class notes Gradebook - ALEKS Initial Assessment #1 - Goulet, Robert signment: ALEKS Initial Assessment #1 mpletion Date: 04/18/11 (time spent: 0 minute adebook Score: 100% ALEKS Corporation's experience with algorithm ALEKS Assessment Report for Goulet, Robert development ensures a commitment to accuracy Course Mastery (209 of 300 Topics) Complex Numbers and Quadratic Equations (6 of 16) als and Rational Exp (5 of 20) and a meaningful experience for students to Arithmetic Read (63 of 63) al Expressions and portions (13 of 35) demonstrate their understanding with a focus Real Numbers and Va (29 of 33) towards online learning. teger Exponents and Polyn (27 of 45) Student Readiness by Topic This ALEKS Assessment report shows the percentage of students that have mastered the following topics Ch.4-Linear Equations in Two Variables The ALEKS[®] Initial Assessment is an artificially A.1
 Reading a point in the coordinate plane
 Plotting a point in the coordinate plane
 Finding a solution to a linear equation in
 Identifying solutions to linear equations intelligent (AI), diagnostic assessment that identifies precisely what a student knows. Graphing a line given the x- and y-inter
Graphing a line given its equation in sl cent form Instructors can then use this information to Graphing a line given its equation in standard form Graphing a vertical or horizontal line izontal line is of a line given the equation in sta make more informed decisions on what topics Graphing a line through a given point with a given slope
 Finding slope given the graph of a line on a grid to cover in more detail with the class. Finding slope given two points on the line ercept of a line ing the slope of a line given its equation 4.5
 Writing the equations of vertical and horizontal lines thro
 Writing equations and drawing graphs to fit a parrative ALEKS is a registered trademark of ALEKS Corporation.

www.successinmath.com



ALEKS[®]

ALEKS is a unique, online program that significantly raises student proficiency and success rates in mathematics, while reducing faculty workload and office-hour lines. ALEKS uses artificial intelligence and adaptive questioning to assess precisely a student's knowledge, and deliver individualized learning tailored to the student's needs. With a comprehensive library of math courses, ALEKS delivers an unparalleled adaptive learning system that has helped millions of students achieve math success.

ALEKS Delivers a Unique Math Experience:

- Research-Based, Artificial Intelligence precisely measures each student's knowledge
- Individualized Learning presents the exact topics each student is most ready to learn
- Adaptive, Open-Response Environment includes comprehensive tutorials and resources
- Detailed, Automated Reports track student and class progress toward course mastery
- Course Management Tools include textbook integration, custom features, and more



The ALEKS Pie summarizes a student's current knowledge, then delivers an individualized learning path with the exact topics the student is most ready to learn.

⁴⁴My experience with ALEKS has been effective, efficient, and eloquent. **Our students' pass rates improved from 49 percent to 82 percent with ALEKS.** We also saw student retention rates increase by 12% in the next course. Students feel empowered as they guide their own learning through ALEKS.³⁷

-Professor Eden Donahou, Seminole State College of Florida

To learn more about ALEKS, please visit: www.aleks.com/highered/math

ALEKS is a registered trademark of ALEKS Corporation.

ALEKS[®] Prep Products

ALEKS Prep products focus on prerequisite and introductory material, and can be used during the first six weeks of the term to ensure student success in math courses ranging from Beginning Algebra through Calculus. ALEKS Prep quickly fills gaps in prerequisite knowledge by assessing precisely each student's preparedness and delivering individualized instruction on the exact topics students are most ready to learn. As a result, instructors can focus on core course concepts and see improved student performance with fewer drops.

⁴⁴ALEKS is wonderful. It is a professional product that takes very little time as an instructor to administer. Many of our students have taken Calculus in high school, but they have forgotten important algebra skills. ALEKS gives our students an opportunity to review these important skills.³⁹

-Professor Edward E. Allen, Wake Forest University



A Total Course Solution

A cost-effective total course solution: fully integrated, interactive eBook combined with the power of ALEKS adaptive learning and assessment.



Students can easily access the full eBook content, multimedia resources, and their notes from within their ALEKS Student Accounts.

To learn more about ALEKS, please visit: **www.aleks.com/highered/math**

Acknowledgments

Manuscript Reviewers and Focus Group Participants

Thank you to all of the dedicated instructors who reviewed manuscript, participated in focus groups, and provided thoughtful feedback throughout the development of the *P.O. W.E. R.* series.

Darla Aguilar, Pima Community College; Scott Albert, College of DuPage; Bhagirathi Anand, Long Beach City College; Raul Arana, Lee College; Jan Archibald, Ventura College; Morgan Arnold, Central Georgia Technical College; Christy Babu, Laredo Community College; Michele Bach, Kansas City Kansas Community College; Kelly Bails, Parkland College; Vince Bander, Pierce College, Pullallup; Kim Banks, Florence Darlington Technical College; Michael Bartlett, University of Wisconsin-Marinette; Sarah Baxter, Gloucester County College; Michelle Beard, Ventura College; Annette Benbow, Tarrant County College, Northwest; Abraham Biggs, Broward College; Leslie Bolinger Horton, Quinsigamond Community College; Jessica Bosworth, Nassau Community College; Joseph Brenkert, Front Range Community College; Michelle Briles, Gloucester County College; Kelly Brooks, Daytona State College (and Pierce); Connie Buller, Metropolitan Community College; Rebecca Burkala, Rose State College; Gail Burkett, Palm Beach State College; Gale Burtch, Ivy Tech Community College; Jennifer Caldwell, Mesa Community College; Edie Carter, Amarillo College; Allison Cath, Ivy Tech Community College of Indiana, Indianapolis; Dawn Chapman, Columbus Tech College; Christopher Chappa, Tyler Junior College; Chris Chappa, Tyler Junior College; Charles Choo, University of Pittsburgh at Titusville; Patricia Clark, Sinclair Community College; Judy Kim Clark, Wayne Community College; Karen Cliffe, Southwestern College; Sherry Clune, Front Range Community College; Ela Coronado, Front Range Community College; Heather Cotharp, West Kentucky Community & Tech College: Danny Cowan, Tarrant County College, Northwest; Susanna Crawford, Solano College; George Daugavietis, Solano Community College; Joseph De Guzman, Norco College; Michaelle Downey, Ivy Tech Community College; Dale Duke, Oklahoma City Community College; Rhonda Duncan, Midlands Technical College; Marcial Echenique, Broward College; Sarah Ellis, Dona Ana Community College; Onunwor Envinda, Stark State College; Chana Epstein, Sullivan County Community College; Karen Ernst, Hawkeye Community College; Stephen Ester, St. Petersburg College; Rosemary Farrar, Southern West Virginia Community & Technical College; John Fay, Chaffey College; Stephanie Fernandes, Lewis and Clark Community College; James Fiebiger, Front Range Community College; Angela Fipps, Durham Technical Community College; Jennifer Fisher, Caldwell Community College & Technical Institute; Elaine Fitt, Bucks County Community College: Carol Fletcher, Hinds Community College: Claude Fortune, Atlantic Cape Community College; Marilyn Frydrych, Pikes Peak Community College; Robert Fusco, Broward College; Jared Ganson, Nassau Community College; Kristine Glasener, Cuyahoga Community College; Ernest Gobert, Oklahoma City Community College; Linda Golovin, Caldwell College; Suzette Goss, Lone Star College Kingwood; Sharon Graber, Lee College; Susan Grody, Broward College; Leonard Groeneveld, Springfield Tech Community College; Joseph Guiciardi, Community College of Allegheny County; Susanna Gunther, Solano College; Lucy

Gurrola, Dona Ana Community College; Frederick Hageman, Delaware Technical & Community College; Tamela Hanebrink, Southeast Missouri State University; Deborah Hanus, Brookhaven College; John Hargraves, St. John's River State College; Michael Helinger, Clinton Community College; Mary Hill, College of DuPage; Jody Hinson, Cape Fear Community College; Kayana Hoagland, South Puget Sound Community College; Tracey Hollister, Casper College; Wendy Houston, Everett Community College; Mary Howard, Thomas Nelson Community College; Lisa Hugdahl, Milwaukee Area Tech College-Milwaukee; Larry Huntzinger, Western Oklahoma State College; Manoj Illickal, Nassau Community College; Sharon Jackson, Brookhaven College; Lisa Jackson, Black River Technical College; Christina Jacobs, Washington State University; Gretta Johnson, Amarillo College; Lisa Juliano, El Paso Community College, Northwest Campus; Elias M. Jureidini, Lamar State College/Orange; Ismail Karahouni, Lamar University; Cliffe Karen, Southwestern College; David Kater, San Diego City College; Joe Kemble, Lamar University; Esmarie Kennedy, San Antonio College; Ahmed Khago, Lamar University; Michael Kirby, Tidewater Community College VA Beach Campus; Corrine Kirkbride, Solano Community College; Mary Ann Klicka, Bucks County Community College; Alex Kolesnik, Ventura College; Tatyana Kravchuk, Northern Virginia Community College; Randa Kress, Idaho State University; Julianne Labbiento, Lehigh Carbon Community College; Robert Leifson, Pierce College; Greg Liano, Brookdale Community College: Charvl Link, Kansas City Kansas Community College; Wanda Long, Saint Charles County Community College; Lorraine Lopez, San Antonio College; Luke Mannion, St. John's University; Shakir Manshad, New Mexico State University; Robert Marinelli, Durham Technical Community College; Lydia Matthews-Morales, Ventura College; Melvin Mays, Metropolitan Community College (Omaha NE); Carrie McCammon, Ivy Tech Community College; Milisa Mcilwain, Meridian Community College; Valerie Melvin, Cape Fear Community College; Christopher Merlo, Nassau Community College; Leslie Meyer, Ivy Tech Community College/Central Indiana; Beverly Meyers, Jefferson College; Laura Middaugh, McHenry County College; Karen Mifflin, Palomar College; Kris Mudunuri, Long Beach City College; Donald Munsey, Louisiana Delta Community College; Randall Nichols, Delta College; Joshua Niemczyk, Saint Charles County Community College; Katherine Ocker Stone, Tusculum College; Karen Orr, Roane State; Staci Osborn, Cuvahoga Community College; Steven Ottmann, Southeast Community College, Lincoln Nebraska; William Parker, Greenville Technical College; Joanne Peeples, El Paso Community College; Paul Peery, Lee College; Betty Peterson, Mercer County Community College; Carol Ann Poore, Hinds Community College; Hadley Pridgen, Gulf Coast State College; William Radulovich, Florida State College @ Jacksonville; Lakshminarayan Rajaram, St. Petersburg College; Kumars Ranjbaran, Mountain View College; Darian Ransom, Southeastern Community College; Nimisha Raval,

Central Georgia Technical College; Amy Riipinen, Hibbing Community College; Janet Roads, Moberly Area Community College; Marianne Roarty, Metropolitan Community College; Jennifer Robb, Scott Community College; Marie Robison, McHenry County College; Daphne Anne Rossiter, Mesa Community College; Anna Roth, Gloucester County College; Daria Santerre, Norwalk Community College; Kala Sathappan, College of Southern Nevada; Patricia Schubert, Saddleback College; William H. Shaw, Coppin State University; Azzam Shihabi, Long Beach City College; Jed Soifer, Atlantic Cape Community College; Lee Ann Spahr, Durham Technical Community College; Marie St. James, Saint Clair County Community College; Mike Stack, College of DuPage; Ann Starkey, Stark State College of Technology; Thomas Steinmann, Lewis and Clark Community College; Claudia Stewart, Casper College; Kim Taylor, Florence Darlington Technical College; Laura Taylor, *Cape Fear Community College;* Janet Teeguarden, *Ivy Tech Community College;* Janine Termine, *Bucks County Community College;* Yan Tian, *Palomar College;* Lisa Tolliver, *Brown Mackie South Bend;* David Usinski, *Erie Community College;* Hien Van Eaton, *Liberty University;* Theresa Vecchiarelli, *Nassau Community College;* Val Villegas, *Southwestern College;* David Walker, *Hinds Community College;* Ursula Walsh, *Minneapolis Community & Tech College;* Dottie Walton, *Cuyahoga Community College;* LuAnn Walton, *San Juan College;* Thomas Wells, *Delta College;* Kathryn Wetzel, *Amarillo College;* Marjorie Whitmore, *North West Arkansas Community College;* Ross Wiliams, *Stark State College of Technology;* Gerald Williams, *San Juan College;* Michelle Wolcott, *Pierce College, Puyallup;* Mary Young, *Brookdale Community College;* Loris Zucca, *Lone Star College, Kingwood;* Michael Zwilling, *University of Mount Union*

Student Focus Group Participants

Thanks to the students who reviewed elements of P.O.W.E.R. and talked candidly with the editorial team about their experiences in math courses.

Eire Aatnite, Roosevelt University; Megan Bekker, Northeastern Illinois University; Hiran Crespo, Northeastern Illinois University; John J. Frederick, Jr., Harold Washington College; Omar Gonzalez, Wright College; Yamizaret Guzman, Western Illinois University; Ashley Grayson, Northeastern Illinois University; Nathan Hurde, University of Illinois at Chicago; Zainab Khomusi, University of Illinois at Chicago; Amanda Koger, Roosevelt University; Diana Kotchounian, Roosevelt University; Adrana Martinez, DePaul University; Laurien Mosley, Western Illinois University; Jeffrey Moy, University of Illinois at Chicago; Jaimie O'Leary, Northeastern Illinois University; Trupti Patel, University of Illinois at Chicago; Pete Rodriguez, Truman College; Kyaw Sint Lay Wu, University of Illinois at Chicago; Shona L. Thomas, Northeastern Illinois University; Nina Turnage, Roosevelt University; Brittany K. Vernon, Roosevelt University; Kyaw Sint Lay Wu, University of Illinois at Chicago

Digital Contributors

Special thanks go to the faculty members who contributed their time and expertise to the digital offerings with P.O.W.E.R.

Jennifer Caldwell, Mesa Community College Chris Chappa, Tyler Junior College Tim Chappell, MCC Penn Valley Community College Kim Cozean, Saddleback College Katy Cryer Cindy Cummins, Ozarks Technical Community College Rob Fusco, Bergen Community College Brian Huyvaert, University of Oregon Sharon Jackson, Brookhaven College Kelly Jackson, Camden County College Theresa Killebrew, Mesa Community College Corrine Kirkbride, Solano Community College Brianna Kurtz, Daytona State College Jamie Manche, Southwestern Illinois College Amy Naughten Christy Peterson, College of DuPage Melissa Rossi, Southwestern Illinois College Janine Termine, Bucks County Community College Linda Schott, Ozarks Technical Community College

From the Authors

The authors would like to thank many people at McGraw-Hill. First, our editorial team: Elizabeth O'Brien, Liz Recker, and most of all, Dawn "Dawesome" Bercier, who believed in, championed, and put never-ending energy into our project from the beginning. To Ryan Blankenship, Marty Lange, Kurt Strand, and Brian Kibby: thank you for your continued support and vision that allows us to help students far beyond our own classrooms. Also, Kim Leistner, Nicole Lloyd, Peggy Selle, Peter Vanaria and Stewart Mattson have been instrumental in what they do to help bring our books and digital products to completion.

We offer sincere thanks to Vicki Garringer, Jennifer Caldwell and Sharon Bailey for their contributions to the series.

From Larry Perez: Thank you to my wife, Georgette, for your patience, support, and understanding throughout this endeavor. Thank you to Patrick Quigley and Candice Harrington for your friendship and support. Also, I must thank Dr. Harriet Edwards and Dr. Raghu Mathur for modeling inspirational and innovative pedagogy, examples which I still strive to emulate.

From Bob Feldman: I am grateful to my children, Jonathan, Joshua, and Sarah; my daughters-in-law Leigh and Julie; my smart, handsome, and talented grandsons Alex and Miles, and most of all to my wife, Katherine (who no longer can claim to be the sole mathematician in our family). I thank them all, with great love.

From Sherri Messersmith: Thank you to my daughters, Alex and Cailen, for being the smart, strong, supportive young women that you are; and to my husband, Phil, for understanding the crazy schedule I must keep that often does not complement your own. To Sue, Mary, Sheila, and Jill: everyone should have girlfriends like you. Thank you to the baristas at my hometown Starbucks for your always-smiling faces at 6 am and for letting me occupy the same seat for hours on end. Larry and Bob, thank you for agreeing to become my coauthors and for bringing your expertise to these books. Bill Mulford, we are immensely grateful for your hard work and creativity and for introducing Bob, Larry, and me in the first place. Working with our team of four has been a joy. And, finally, thank you Bill, for your friendship, your patience, and for working with me since the very beginning more than 8 years ago, without question the best student I've ever had.

Sherri Messersmith Larry Perez Bob Feldman

Application Index

BIOLOGY AND HEALTH

ages of mother and daughter, 227 ages of sisters, 268 antibiotic remaining in system, 729 bacteria population in culture, 763-764, 771–772, 775, 785 blood alcohol percentage, 153 cats and dogs treated per day, 287 distance person can see to horizon, 586 dog licenses issued per year, 742 drivers in fatal vehicle accidents 152 foot length and shoe size, 184 generic vs. name brand drugs, 93 ibuprofen in bloodstream over time, 213 intravenous drip rate, 484 iodine in system, 776 length of hair, 147-149 medication dosage by weight, 484 peanut allergies treated per year, 739-740 spending on veterinary care, 91 steroid solution, 85

BUSINESS AND MANUFACTURING

billboard rentals, 184 dimensions of bulletin board, 409, 838 dimensions of desktop, 403 gold production by country, 267-268 hybrid vehicles sold, 132 manufacturing cost of notebooks, 495 market share of paper towel brands, 271 market share of tire brands, 287 production cost of clay pigeons, 690 production cost of purses, 690 profit function, 690, 699 profit on book sales, 319-320 profit on purse sales, 470 revenue during construction, 91 salary and commission over time, 168-169 Starbucks worldwide, 64 time to assemble conference notebooks, 486 time to put away clothes, 697 value of U.S. exports, 150

CONSTRUCTION AND WORK

area of Big Ben clock face, 72 area of ice rink, 678 area watered by sprinklers, 73 boards used for playhouse, 289 bridge arch, 816 cost to carpet room, 490 dimensions of cardboard for box, 647–648, 651, 698 dimensions of countertop, 417 dimensions of dog pen, 679 dimensions of door, 269 dimensions of garden, 403, 623, 678 dimensions of glass, 409

dimensions of lot, 261-262 dimensions of Parthenon fover, 485 dimensions of playground, 269 dimensions of sheet metal, 651 dimensions of storage cube, 524 distance from ceiling of light fixture, 652 distance from ground of shirt on clothesline, 652 distance from ladder to wall, 410 farmland in county, 64 fencing for trapezoidal plot, 73 height of wall with ladder, 622 length of fence for animal pen, 406 length of gravel road, 91 length of pool, 72 length of room, 66-67 length of trapezoidal plot, 73 length of wire attached to pole, 407, 410 lengths of boards, 54-55, 65 lengths of cables, 65 lengths of chain, 55 lengths of pipes, 63 lengths of trim pieces, 63 lengths of wires, 62 maximum dimensions of outdoor café, 698 maximum fenced area, 670-671, 679 Oval Office equation, 816 radius of garden, 524 reinforcing the Leaning Tower of Pisa, 153 slope of a driveway, 167 slope of a highway, 157 slope of a parking garage ramp, 167 slope of a roof, 167 slope of a wheelchair ramp, 167 storage capacity of container, 809 time for ice to reach ground, 524 time to assemble swing set, 506 time to build tree house, 644 time to clean carpets, 504 time to clean pool, 486 time to fertilize lawn, 486 time to mow lawn, 484 time to paint bedroom, 482-484 time to paint billboard, 486 time to paint fence, 486 time to shovel snow, 486 time to trim bushes, 486 weight supported by beam, 496 width of pond border, 648-649 width of window shade, 129

CONSUMER APPLICATIONS

American vs. foreign cars, 91 appreciation of home value, 728–729 bouquet supply and demand, 698 break-even point for backpacks, 838 capacity of conical vase, 586 children at birthday party, 105–106 cost of attorney consultation, 801 cost of batteries, 484 cost of car rental, 248 cost of car washes, 270 cost of earrings and necklace, 263 cost of gasoline, 212, 479 cost of library rate postage, 797 cost of mailing large envelope, 797 cost of mailing small packages, 801 cost of metered parking, 801 cost of souvenirs, 270 cost of truck rental, 108, 248 depreciation of car value, 726, 728, 783 depreciation of truck value, 726 dimensions of rug, 409, 586 dimensions of storage box, 409 gallons of ethanol purchased, 79-80 hybrid vehicle registrations over time, 185 loudness of dishwasher, 763 maximum guests at inn, 678 moon jump rental, 152 motel rooms with queen size beds, 261 number of restaurants in U.S., 268 original price of backpack, 64 original price of book, 63 original price of calendar, 63 original price of coffee maker, 64 original price of refrigerator, 64 pages in book, 65 parking garage time limits, 108 personal consumption expenditures over time, 223 price of birthday gifts, 128-129 profit on dog house sales, 323 profit on toaster sales, 323 sale price of bathing suit, 63 sale price of clothing, 717 sale price of dress shirt, 58 sale price of jeans, 58 sale price of stroller, 63 sales of wine, 698 sales tax on clothing, 717 shovel supply and demand, 652 time to address invitations, 486 types of batteries purchased, 270 types of books sold, 480 types of stamps purchased, 83, 270 value of car over time, 167

DISTANCE AND TRAVEL

airport on-time departures, 286 cruise ships operating in North America, 349 distance between car and motorcycle, 418 distance between cyclists, 410 distance driven, 81 distance from home, 411 distance from LA to Chicago, 153 distance on bike, 64 distance space shuttles travel, 312 distance to California, 62 distance traveled by jet, 225 distance traveled by sloth, 312 distance traveled by truck, 211 fuselage of Boeing 767, 816 height of dropped rock, 411 height of launched object, 411, 412, 418 height of rocket, 690 height of thrown object, 408 kinetic energy of car, 495 loudness of jet takeoff, 785 maximum height of ball, 669-670 maximum height of object, 670, 678, 698 passengers on New York flight, 62 speed during snowstorm, 644 speed of boat in current, 485 speed of boat in still water, 481-482, 485, 644 speed of car. 85 speed of current, 485, 486, 504 speed of driver at time of accident, 524 speed of plane in wind, 485, 486, 504, 644 speed of planes, 85 speed of walker, 486 speeds of car and bus, 287 speeds of car and train, 134, 271 speeds of car and truck, 270 speeds of cyclists, 265-266, 271 speeds of drivers, 83, 84 speeds of planes, 84, 271 speeds of trains, 84, 270 speeds of walker and cyclist, 271 students biking to class, 62 taxi charges per mile, 108 time for ball to reach ground, 629-630, 632 time for ball to reach height, 629-630, 632, 669-670 time for object to reach ground, 630, 632, 651, 698 time for object to reach height, 630, 632, 651, 670, 678, 698 time to catch up, 81-83, 84, 85, 92 time to meet, 93 time to travel distance, 495 time until distance apart, 84, 85 velocity of an object, 211 velocity of car, 544

EDUCATION

average salary for high school principals, 185 boys and girls in class, 53–54 children not in preschool, 91 freshman in class, 65 number of students over years, 160 per-pupil spending, 154 revenue from t-shirt fundraiser, 412 students giving speeches *vs.* writing papers, 269 students studying French and Spanish, 287 students taking notes in pen *vs.* pencil, 485 test average in class, 62, 108 time to grade tests, 644

ENTERTAINMENT

album downloads per year, 287 albums sold per artist, 65 *American Idol* viewers, 150 Broadway play attendees, 652 CD sales per artist, 91 cost of concert tickets, 262-263, 269 cost of movie tickets, 271 cost of theater seats, 287 Country Music Awards won, 269 dimensions of television screen, 651 earnings of two movies, 65 Emmy nominations by network, 260-261 movies nominated for Academy Awards, 268 original price of CD, 58-59 original price of video game, 59 profit on television sales, 323 revenue from comedy performance, 412 revenue from theater tickets, 490 revenue from ticket sales, 412 sale price of television, 63 types of movie tickets sold, 83, 85

ENVIRONMENT AND NATURE

altitude and barometric pressure, 153-154 area of oil spill, 717 average temperature in Tulsa, 717 carbon emissions per person, 312 cockroach population increase, 729 deer in wildlife refuge, 485 difference between elevations, 18 difference between temperatures, 15 elevation of city, 18 equivalent temperatures, 75 farms with milk cows, 185 gallons of water in water treatment plant, 213 garbage collected per year, 740 highest temperature in U.S., 18 lengths of rivers, 63 lowest temperature in Colorado, 18 pollution produced by population, 495 quills on porcupine, 349 radius of oil spill, 717 spread of magnetic stripes, 471 sulfur dioxide emissions over time, 180-181 temperatures in Anchorage, 54 weights of dogs, 63 wind chill, 533, 586

FINANCE AND INVESTMENT

average earnings for embalmers, 212 average salary for pharmacists over time, 169 compound interest on account, 759, 763, 785 compound interest on loan, 763 continuous compounding, 760, 763, 770–771, 775, 785 difference in median income, 18 earnings at part-time job, 212 earnings per week, 495 exchange rate between dollars and pesos, 169 income and hours worked, 169 interest earned on annuity, 729 interest earned on investment, 60, 64, 493 interest on two accounts, 64 interest rate needed, 775, 785 investments in three accounts, 65 investments in two accounts, 60-62, 64, 65, 91, 270, 485 net weekly pay, 783 salary over time, 64 salary per year, 65 value of stock over time, 222 wealthiest women in the world, 116

FOOD

caffeine in soda, 484 calories in ice cream, 227 calories in mayonnaise brands, 271 candy mixture, 287 chicken consumption per capita, 269 coffee blend, 84 cookie sales per month, 742 cost of cantaloupe and watermelon, 270 cost of chips and soda, 700 cost of granola, 484 cost of hamburger and fries, 270 cost of hot dog, fries, and soda, 271 cost of hot dog and soda, 287 cost of ice cream cone, shake, and sundae, 287 cost of meals, 269 cost of nut mixture, 270 cost of potatoes, 478-479 fat in Starbucks drink, 504 fruit juice mixture, 270 grams of protein in protein bars, 271 guacamole eaten during Super Bowl, 312 height of coffee can, 73 height of tomato sauce can, 73 length of candy bar, 419 milk consumption per capita, 169 nut mixture, 84 original price of dog food, 93 ounces in cereal box, 128 ounces in milk container, 128 ounces in soup can, 125 potato chips consumed per person, 152 profit on candy sales, 320 profit on salmon sales, 470 sales of dog food, 784 sales of hamburgers, 62 sandwich supply and demand, 652 sodium in drinks, 287 sugar in drinks, 62, 270 types of coffee ordered, 479–480 types of flour in mixture, 485 volume of soup can, 586

INTERNET AND TECHNOLOGY

dimensions of computer screen, 838 dimensions of iPod, 269 dimensions of laptop screen, 623 dimensions of monitor, 287 dimensions of mouse pad, 262 DVD data transfer rate, 212 Google quarterly revenue, 289 households with Internet access, 247 ink droplets per photo print, 312 length of copy machine paper, 72 original price of camera, 63 original price of cell phone, 65 profit on calculator sales, 323 profit on laptop sales, 323 sale price of cell phone, 63 sales of digital cameras, 700 samples of sound read from CD, 207-208, 212 surface area of CD, 809 text messages per month, 106 texts per person per day, 287 time for programming job, 486 time to print pictures, 486

time to set up alarm system, 486 USB data transfer rate, 225 width of printed area, 72 wireless communication subscribers over time, 223 YouTube video views, 289

SCIENCE AND CHEMISTRY

acid solution, 80-81, 84, 92, 265, 270 alcohol solution, 81, 84, 270, 287, 352, 506,851 antifreeze solution, 84 cleaning solution, 485 current in circuit, 492 dimensions of aquarium, 409 focal length of lens, 470 force exerted on object, 495 force to stretch spring, 496 frequency of piano string, 495 height of firework shell, 411–412 height of tank, 72 hydrogen peroxide solution, 84, 264-265 illuminance, 652 impedance of circuits, 586 intensity of light, 492 loudness of space shuttle, 763 mass of water molecules, 349 period of pendulum, 524 pH of substances, 764, 785 power in electrical system, 495 power generated by Hoover Dam, 312 radioactive decay, 772-773, 775-776, 785 radius of water tank, 552 resistance of wire, 495 silver alloy, 85 speed of sound, 586 surface area of cube, 495 time to empty tank, 644 time to fill pool, 644

time to fill sink, 486 time to fill tub, 486 volume of box, 493 volume of candle wax, 552 volume of cylinder, 495, 586 volume of gas, 504 wave velocity, 586, 604 weight of ball, 504 weight of object above Earth, 496

SOCIOLOGY AND DEMOGRAPHICS

addresses of houses, 63 areas of countries, 62 babies born to teen mothers, 168, 678 change in housing starts, 18-19 females in Belgian workforce, 186 fingerprint comparisons per second, 212 households with pets, 485 increase in housing, 742 maximum traffic tickets written, 678 men in civilian labor force over time, 169–170 population change in Oakland, 19 population decrease, 775 population increase, 775, 785 population of Maine over time, 184–185 population of North Dakota over time, 185 tourism-related output in U.S., 649-650 tourists visiting per year, 742 violent crimes in U.S., 678 voters for each candidate, 63, 485

SPORTS AND HOBBIES

break-even point for basketballs, 838 colors in paint mixture, 485 cost of baseball tickets, 271 cost of football tickets and parking, 270 cost of soccer uniforms, 349 difference between golf scores, 15 difference in baseball attendance, 18

dimensions of bandana, 417 dimensions of fabric pieces, 651 dimensions of Ferris wheel, 809 dimensions of London Eye, 809 dimensions of painting, 409 dimensions of picture, 269 dimensions of sail, 651 female motocross spectators, 484 height of baseball, 407-408 height of bike ramp, 417, 651 length of kite string, 623 length of side of die, 524 lengths of jump ropes, 63 loudness of basketball game, 785 markup on fishing poles, 65 NBA championships won, 114 NCAA championships won, 269 NCAA championship viewers, 269 number of male runners, 62 Olympic medals per country, 63 Olympics participants, 64 pitchers on baseball team, 62 profit on bicycle sales, 323 racing winnings over time, 18 revenue of basketball teams, 271 schools in NCAA conferences, 717 snowboarding and ice skating participants, 246-247

soccer games played in season, 65 speed of baseball pitch, 133 speed of runner, 644 Super Bowl net yardage, 18 teams playing in Rose Bowl, 268 time to cut out shapes, 486 width of basketball lane, 73 width of picture frame border, 651 width of pillow sham border, 698 width of ping-pong table, 67 width of swimming pool border, 651

CHAPTER

Real Numbers and Algebraic Expressions



OUTLINE

Study Strategies: The P.O.W.E.R. Framework

- 1.1 Sets of Numbers
- 1.2 Operations on Real Numbers
- **1.3** Exponents, Roots, and Order of Operations
- 1.4 Algebraic Expressions and Properties of Real Numbers

Group Activity

emPOWERme: Why Am I Going to College?

Math at Work:

Computer Game Designer

Ever since he was a child, Dave Cantelmo has known what he wanted to do: create video games. "I still remember playing games on the classic systems I had growing up," Dave says. "I would spend hours and hours playing those games and always imagined the games I wanted to create myself one day."

In order to realize his ambitions, Dave put in the time and effort necessary to learn the design and computer programming skills involved in video game development. Early on in college, he was particularly focused on building up his math abilities, as math is critical to the technical side of video game creation. "I was always a little intimidated by math," Dave describes. "But with hard work and the help of my instructors, I was able to turn math into one of my strengths. Now, it's something I use in my job every day."

Creating a successful video game is a complex challenge. "Completing a video game takes the coordinated efforts of dozens of designers, writers, programmers, animators, and many other people, all working for years to turn an idea into a game people all over the world can play," Dave explains. He says the key to completing such a difficult task is taking a smart, organized approach, dividing the work into steps that will culminate in the finished product.

In this chapter, we will discuss the topic of real numbers. We will also introduce P.O.W.E.R., a framework that can help you succeed in the complex challenges you face, either in the classroom, on the job, or in your daily life.

EOWER Study Strategies The POWER. Framework

The P.O.W.E.R. Framework is based on an acronym—a word formed from the first letters of a series of steps. P.O.W.E.R. stands for Prepare, Organize, Work, Evaluate, and Rethink. That's it. It's a simple framework, but an effective one. P.O.W.E.R. gives you a proven, ready-to-use approach to virtually any challenge you face, from studying for a math test to developing a presentation for your coworkers to writing the family grocery list. Think of its steps as a roadmap to success no matter what your task is.

Whether you are familiar with the P.O.W.E.R. framework already or are encountering it for the first time, take a moment now to review each of its steps in depth:

D Prepare

- Think about what you are trying to accomplish: Define both your short-term and long-term goals.
- Long-term goals are major accomplishments that take a significant amount of time and effort to achieve, such as graduating from college. Short-term goals are steps that are easier to accomplish and bring you closer to your long-term goals—for example, doing well on a math exam.
- Identify the tools you will need to complete your task.
- Effective organization involves gathering both the *physical* tools you will need to complete your task (for example, a textbook, pen, paper, and so forth) and doing the *mental* work (reviewing lecture notes or major concepts in your textbook, say) to ensure you are ready to succeed.

Work

- With the previous steps as your foundation, do the work of completing your task.
- When doing math tasks in particular, it is important to work efficiently but patiently, neither trying to rush through the work nor becoming frustrated and giving up after the first difficulty you encounter.
- Stay motivated by keeping your goals in mind.

匡 Evaluate

- Think back to your goal for the task. Did you meet your own expectations?
- Revise your work based on your assessment of it.
- In math courses, it's important to identify the specific obstacles that may be causing you to perform below your capabilities. Are there particular concepts you are struggling with? Would you benefit from working with a math tutor or your fellow students?

R Rethink

- Think critically about both the work you have done and the process you used to complete it. What did you do that worked well? Where do you see room for improvement?
- Take a step back and consider how the task you completed brought you closer to your long-term goals.



Chapter 1 Plan

Prepare Organize			
What are your goals for Chapter 1?	How can you accomplish each goal?		
1 Be prepared before and during class.	 Don't stay out late the night before and be sure to set your alarm clock! Bring a pencil, notebook paper, and textbook to class. Avoid distractions by turning off your cell phone during class. Pay attention, take good notes, and ask questions. Complete your homework on time and ask questions on problems you do not understand. 		
2 Understand the homework to the point where you could do it without needing any help or hints.	 Read the directions and show all of your steps. Go to the professor's office for help. Rework homework and quiz problems and find similar problems for practice. 		
3 Use the P.O.W.E.R. framework to help you organize your study: Why Am I Going to College?	 Read the Study Strategy that explains how to use P.O.W.E.R. What does P.O.W.E.R. stand for? Complete the emPOWERme that appears before the Chapter Summary. 		
4 Write your own goal.	•		
What are your objectives for Chapter 1?	How can you accomplish each objective?		
1 Learn the different sets of numbers.	Learn the definitions in Section 1.1.Take good notes in class.		
2 Be able to add, subtract, multiply, and divide real numbers.	• Master the steps for these operations! Future sections build on this knowledge, so continually review these operations.		
3 Understand how to evaluate expressions, roots, and exponents. Be able to simplify an expression using the order of operations.	 Understand the meaning of exponents and how to identify the base and exponent. Memorize the powers of integers in Section 1.3. Learn the Order of Operations: Use Please Excuse My Dear Aunt Sally to help you remember the order of operations. 		
4 Understand the properties of real numbers and how they can be used to simplify problems.	 Understand the meaning of each property based on the meaning of the word. (Commutative property = "commute.") Be aware of when the properties can be used to help simplify a problem. 		
5 Write your own goal.	•		

Work Read Sections 1.1 to 1.4, and complete the exercises.				
Evaluate Complete the Chapter Review and Chapter Test. How did you do?	 Rethink How did you perform on the goals for the chapter? Which steps could be improved for next time? If you had the chance to do this chapter over what would you do differently? Think of a job you might like to have and describe how you would need to use what you have just learned to effectively do that job. How has the P.O.W.E.R. framework helped you master the objectives of this chapter? Where else could you use this framework? Make it a point to use P.O.W.E.R. to complete another task this week. 			

1.1 Sets of Numbers

Prepare	O rganize		
What are your objectives for Section 1.1?	How can you accomplish each objective?		
1 Identify Numbers and Graph Them on a Number Line	 Know the definition of <i>natural numbers, whole numbers, integers, rational numbers,</i> and <i>irrational numbers.</i> Determine when a number may belong to more than one number set. Know how to draw/label a number line and determine where that number should be graphed. Complete the given examples on your own. Complete You Trys 1, 2, and 3. 		
2 Compare Numbers Using Inequality Symbols	 Write the inequality symbols in math notation and in words. Know how to determine the larger of two given numbers. Complete the given examples on your own. Complete You Trys 4 and 5. 		
3 Find the Absolute Value of a Number	 Know the definitions of <i>additive inverse</i> and <i>absolute value</i>. Be able to show, on a number line, the <i>additive inverse</i> and the <i>absolute value</i> of a given number. Complete the given examples on your own. Complete You Trys 6 and 7. 		



Read the explanations, follow the examples, take notes, and complete the You Trys.

1 Identify Numbers and Graph Them on a Number Line

Why should we review sets of numbers and arithmetic skills? Because the manipulations done in arithmetic are precisely the same set of skills needed to learn algebra. Let's begin by defining some numbers used in arithmetic:

The set of natural numbers is $\{1, 2, 3, 4, 5, \ldots\}$.

The set of whole numbers is $\{0, 1, 2, 3, 4, 5, ...\}$.

Natural numbers are often thought of as the counting numbers. Whole numbers consist of the natural numbers and zero. Let's look at other sets of numbers. We begin with integers. Remember that, on a number line, positive numbers are to the right of zero, and negative numbers are to the left of zero.

Definition

The set of **integers** includes the set of natural numbers, their negatives, and zero. The set of *integers* is $\{..., -3, -2, -1, 0, 1, 2, 3, ...\}$.



Notice in Example 2 that $\frac{2}{3}$ did not belong to any of these sets. That is because the whole numbers, natural numbers, and integers do not contain any fractional parts. $\frac{2}{3}$ is a *rational number*.

W Hint

Remember that whole numbers, natural numbers, and integers can all be written in the form $\frac{p}{q}$ where q = 1.

Definition

A rational number is any number of the form $\frac{p}{q}$, where p and q are integers and $q \neq 0$.

In other words, a rational number is any number that can be written as a fraction where the numerator and denominator are integers and the denominator does not equal zero.

Rational numbers include much more than numbers like $\frac{2}{3}$, which are already in fractional form. They also include numbers such as 3, 0.5, -7, 0.4, and the square root of 9 because each of these numbers can be written as a fraction.

To summarize, the set of rational numbers includes

- 1) integers, whole numbers, and natural numbers.
- 2) repeating decimals.
- 3) terminating decimals.
- 4) fractions and mixed numbers.

The set of rational numbers does *not* include nonrepeating, nonterminating decimals or radicals like $\sqrt{5}$ where the radicand is *not* a perfect square. These numbers cannot be written as the quotient of two integers. Numbers such as these are called *irrational numbers*.

W Hint Note that it is not possible to write an irrational number as a fraction. Some irrational numbers

are π , $\sqrt{5}$, 0.412738...

Definition

The set of numbers that cannot be written as the quotient of two integers is called the set of **irrational numbers**. Written in decimal form, an *irrational number* is a nonrepeating, nonterminating decimal.

If we put together the sets of numbers we have discussed up to this point, we get the *real numbers*.

Definition

The set of real numbers consists of the rational and irrational numbers.

We summarize the information next with examples of the different sets of numbers:



From the figure we can see, for example, that all whole numbers $\{0, 1, 2, 3, ...\}$ are integers, but not all integers are whole numbers (-3, for example).

EXAMPLE 3	Given the set of numbers $\left\{0.\overline{2}, 37, -\frac{4}{15}, \sqrt{11}, -19, 8.51, 0, 6.149235\right\}$, list the				
	a) integers b) natural numbers c) whole numbers				
	d) rational numbers e) irrational numbers f) real numbers				
	Solution				
	a) integers: -19, 0, 37				
	b) natural numbers: 37				
	c) whole numbers: 0, 37				
	d) rational numbers: $0.\overline{2}$, 37, $-\frac{4}{15}$, -19, 8.51, 0 Each of these numbers can be				
	written as the quotient of two integers.				
	e) irrational numbers: $\sqrt{11}$, 6.149235 These numbers <i>cannot</i> be written as the quotient of two integers.				
	f) real numbers: All of the numbers in this set are real.				
	$\left\{0.\overline{2}, 37, -\frac{4}{15}, \sqrt{11}, -19, 8.51, 0, 6.149235\right\}$				
YOU TRY 3	Given the set of numbers $\left\{-38, 0, \sqrt{15}, 6, \frac{3}{2}, 5.4, 0.\overline{8}, 4.981162\right\}$, list the				
	a) whole numbers b) integers c) rational numbers				
	d) irrational numbers				

Real Numbers

2 Compare Numbers Using Inequality Symbols

Let's review the inequality symbols.

Note

< less than	\leq less than or equal to
> greater than	\geq greater than or equal to

 \neq not equal to \approx approximately equal to

We use these symbols to compare numbers as in 5 > 2, $6 \le 17$, $4 \ne 9$, and so on. How do we compare negative numbers?

As we move to the left on the number line, the numbers get smaller. As we

🚾 Hint

Think about why -8 is less than -7 on a number line. Draw a number line and notice that -8 is to the left of -7.

EXAMPLE

Insert $>$ or $<$ to	o make the statement true	e. Look at the num	per line, if necessary.
	-5-4-3-2-1	0 1 2 3 4 5	
a) 5 <u>1</u>	b) -4 _ 3 c)	-15	d) -52
Solution			
a) 5 <u>></u> 1	5 is to the right of 1.	b) -4 <u><</u> 3	-4 is to the left of 3.
c) $-1 \ge -5$	-1 is to the right of -5 .	d) −5 <u><</u> −2	-5 is to the left of -2 .

move to the *right* on the number line, the numbers get larger.

YOU TRY 4Insert > or < to make the statement true.a)
$$4 _ 9$$
b) $6 _ -8$ c) $-3 _ -10$

We use signed numbers in everyday situations.

EXAMPLE 5

Use a signed number to represent the change in each situation.

- a) After a storm passed through Kansas City, the temperature dropped 18°.
- b) Between 2006 and 2010, retail sales of gluten-free products rose by \$1.3 billion. (www.celiac.com)

Solution

- a) -18° The negative number represents a decrease in temperature.
- b) \$1.3 billion The positive number represents an increase in sales.

YOU TRY 5 Use a signed number to represent the change. After taking his last test, Julio raised his average by 3.5%.

3 Find the Absolute Value of a Number

Before we discuss absolute value, we will define additive inverses.

Distance = 2 Distance = 2

$$-5 - 4 - 3 - 2 - 1$$
 0 1 2 3 4 5

Notice that both -2 and 2 are a distance of 2 units from 0 but are on opposite sides of 0. We say that 2 and -2 are *additive inverses*.

W Hint

Notice that the additive inverse of a negative number is always positive. For a positive number, the additive inverse is always negative.

Definition

Two numbers are **additive inverses** if they are the same distance from 0 on the number line but on the opposite sides of 0. Therefore, if a is any real number, then -a is its additive inverse.

Furthermore, -(-a) = a. We can see this on the number line.



This idea of "distance from zero" can be explained in another way: absolute value.

Definition

If a is any real number, then the **absolute value of** a, denoted by |a|, is

i) $a \text{ if } a \ge 0$ ii) -a if a < 0

Remember, |a| is never negative.



The absolute value of a number is the distance between that number and 0 on the number line. It just describes the distance, *not* what side of zero the number is on. Therefore, the absolute value of a number is always positive or zero.